Last time: Gaussian Elim Solution Paradigms A linear System has 3 possible solution paradigms: -> No solutions * (from an inconsistent equation) -> Exactly 1 Solition & -> Infinitely many solutions - X This These are the only three possibilities... Goal: Determine Soldin Sets. Grave Soldins as Glum vectors. In general me give a fill set of Golumn vectors. Ex: Last the he solved $\begin{cases} 2 \times & +2 + h = 5 \\ 3 \times & -2 - h = 0 \\ 4 \times & +9 + 22 + h = 9 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \\ 7 = 5 - t \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases} x = 0 \\ y = -1 + t \end{cases} \qquad \begin{cases} x = 0 \end{cases} \qquad \begin{cases}$ we write the solution set like so: $\begin{bmatrix} 0 \\ -1 + t \\ 5 - t \\ t \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \\ 5 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ t \\ -t \\ t \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \\ 5 \\ 0 \end{bmatrix} + t \begin{bmatrix} 0 \\ 1 \\ -1 \\ 1 \end{bmatrix} + t \begin{bmatrix} 0 \\ 1 \\ -1 \\ -1 \end{bmatrix} + t \begin{bmatrix} 0 \\ 1 \\ -1 \\ -1 \end{bmatrix} + t \begin{bmatrix} 0 \\ 1 \\ -1 \\ -1 \end{bmatrix} + t \begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix} + t$

MB: this vector is a particular solution ...

Matrices

A matrix is a rectangular array of numbers

$$\begin{bmatrix} 2 & 2 \\ 1 & 5 \\ 1 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 3 & 2 \\ 1 & 0 \end{bmatrix}$$

$$2 \times 2$$

$$\begin{bmatrix} 3 & 2 \\ 1 & 0 \end{bmatrix}$$

An mxn matrix has m rows an n columns

A von vector is an NXI matrix.

A von vector is a IXN matrix.

The entries of a matrix are the numbers in the matrix Entries are indexed by row and column.

Convention: Matrices are represented u/ Capital letters the corresponding entries are repid by the lowercase letter, so $\mathcal{D} = \left[d_{i,j} \right].$

We can represent a linear system via an arguentel matrix. $Ex: \begin{cases} 3x + 59 - 72 + w = 0 \\ 59 - 32 + v = 5 \\ x - 2 = 6 \end{cases} \begin{bmatrix} 3 & 5 - 7 & 1 & 0 \\ 0 & 5 & -3 & 1 & 5 \\ 1 & 0 & -1 & 0 & 6 \end{bmatrix}$

Let's solve this system n/ its matrix representation

NB: Gassian elimination translates into "ron operations" for the matrix setup. Sol: [3 5 -7 1 0] (3 4) [1 0 -1 0 6]

[0 5 -3 1 5]
[0 5 -3 1 5]

[1 0 -1 0 6]
[2 "cho"] "first nonzero entry of each row is a 1 "Reduced Ron Echelon and sees only 0's above and below" Form" $\begin{cases} x = 29 \\ y = 74 - \frac{1}{5}t \\ z = 23 \\ w = 74 - 5s \end{cases}$ or $\begin{cases} x = 29 \\ y = 5 \\ w = 74 - 5s \end{cases}$ (lence he has solition set $\begin{cases} 29 \\ 74 \\ 5 \\ 23 \end{cases}$; $t \in \mathbb{R}$) OR $\begin{cases} 29 \\ 0 \\ 23 \\ 74 \end{cases} + S \begin{bmatrix} 0 \\ 0 \\ -5 \end{bmatrix}$: SER $\begin{cases} 29 \\ 50me \\ 50th Set \\ 6mm \end{cases}$

Ex: Solve
$$\begin{cases} x_1 - x_2 + 2x_3 = 4 \\ x_1 - x_2 + 5x_3 = 17 \end{cases}$$

Sol: $\begin{cases} 0 & 0 & 1 & 4 \\ 4x_1 - x_2 + 5x_3 = 17 \end{cases}$
 $\begin{cases} x_1 & 1 \times 3 = 4 \\ 4 - 1 & 5 & 17 \end{cases}$
 $\begin{cases} x_1 & 1 \times 3 = 4 \\ x_2 & - x_3 = -1 \end{cases}$

Solve $\begin{cases} x_1 & 1 \times 3 = 4 \\ x_2 & - x_3 = -1 \end{cases}$

Solve $\begin{cases} x_1 & 1 \times 3 = 4 \\ x_2 & - x_3 = -1 \end{cases}$

Ex: Solve $\begin{cases} 3x + 2y = 5 \\ 6x - 4y = 0 \end{cases}$

Sol: $\begin{cases} 3 & 2 & 5 \\ 6x - 4y = 0 \end{cases}$

Sol: $\begin{cases} 3 & 2 & 5 \\ 6x - 4y = 0 \end{cases}$

Sol:
$$\begin{bmatrix} 3 & 2 & 5 \\ -6 & -4 & 0 \end{bmatrix}$$
 $\begin{bmatrix} 2 & 21 \\ 0 & 0 & | 10 \end{bmatrix}$ $=$

So the Solution set is $\emptyset = \{3\}$ tempty set.

Preview of Coming Attactions: Matrix Algebra. Operations on natrices (today): -> Normal row operations (Smap, all, moltiply). Defn: Let A and B be mxn matrices
and let c ER be constant. The Sum of A and B is $A+B = [a_{ij}+b_{ij}],$ i.e. the matrix obtained by entry-wise addition.

The Scalar multiple of A by (is $cA = [ca_{ij}],$ i.e. the matrix obtained from multiplying each entry
of A by C.

 $EX: \begin{bmatrix} 3 & -1 & 0 \\ 2 & 0 & 1 \end{bmatrix} + \begin{bmatrix} 7 & -1 & 0 \\ 0 & -1 & -1 \end{bmatrix} = \begin{bmatrix} 3+1 & -1-1 & 0+0 \\ 2+0 & 0-1 & 1-1 \end{bmatrix} = \begin{bmatrix} 10 & -2 & 0 \\ 2 & -1 & 0 \end{bmatrix}$ $S\begin{bmatrix} 2 & 3 \\ 1 & -3 \end{bmatrix} = \begin{bmatrix} 5 \cdot 2 & 5 \cdot 3 \\ 5 \cdot 1 & 5 \cdot -3 \end{bmatrix} = \begin{bmatrix} 10 & 15 \\ 5 & -15 \end{bmatrix}$ $MM-EX: \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 5 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \\ 7 & -2 \end{bmatrix}$ TS UNDEFINED!